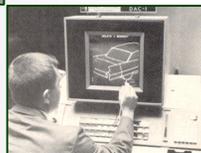




Chap. 7

Illumination-based Shading



Ensino de Informática (3326) - 4º ano, 2º semestre
Engenharia Electrotécnica (2287) - 5º ano, 2º semestre
Engenharia Informática (2852) - 4º ano, 2º semestre



Lighting Review

■ Lighting Models

- Ambient
 - Normals don't matter
- Lambert/Diffuse
 - Angle between surface normal and light
- Phong/Specular
 - Surface normal, light, and viewpoint



Applying Illumination

- We now have an direct illumination model for *a single point* on a surface
- Assuming that our surface is defined as a mesh of polygonal facets, *which points should we use?*
 - Computing these models for every point that is displayed is expensive
 - Normals may not be explicitly stated for every point
- Keep in mind:
 - It's a fairly expensive calculation
 - Several possible answers, each with different implications for the visual quality of the result



Shading Models

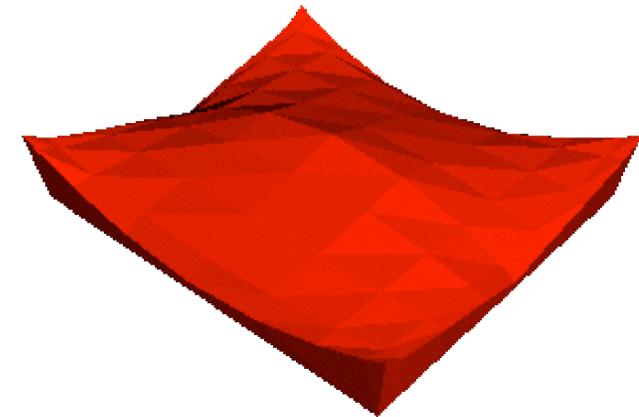
- Several options:

- Flat** shading
- Gouraud** shading (interpolation)
- Phong** shading (interpolation)

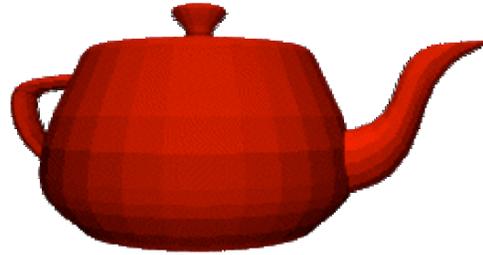
- New hardware does per-pixel programmable shading!

Flat (or Constant) Shading

- The simplest approach, *flat shading*, calculates illumination at a single point for each polygon.
 - OpenGL uses one of the vertices
- The illumination intensity (color) is the same for all points of each polygon.
- Advantages:
 - Fast - one shading value computation per polygon
- Disadvantages:
 - Inaccurate
 - Artifacts: Discontinuities at polygon boundaries



Is flat shading realistic for faceted object?

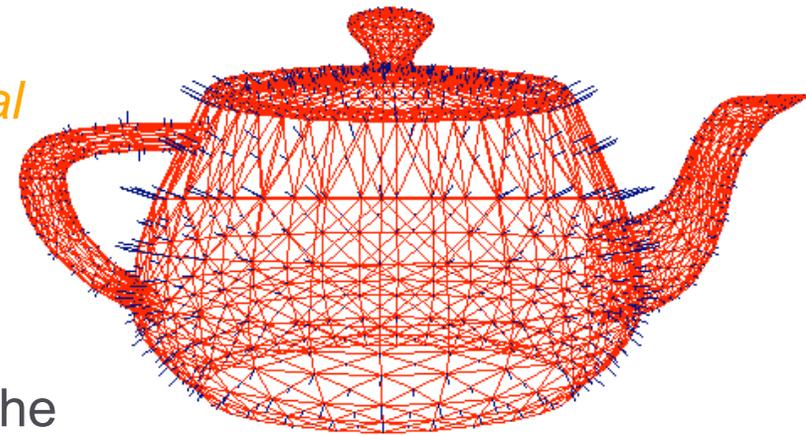
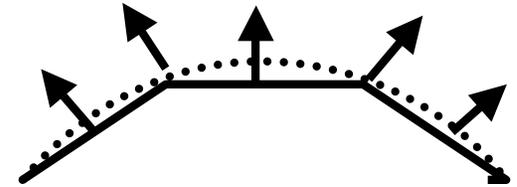


NO!

- For point sources, the direction to light varies across the facet
- For specular reflectance, direction to eye varies across the facet

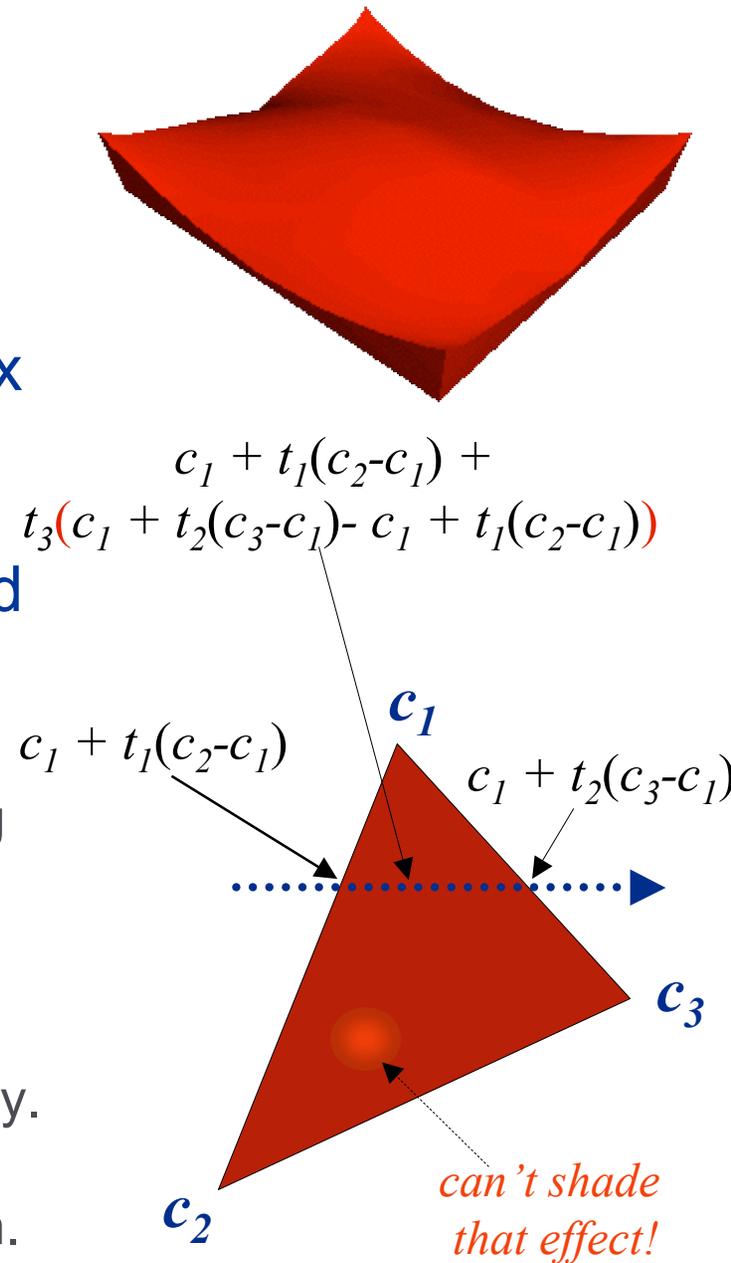
Flat Shading

- We can refine it a bit by evaluating the Phong lighting model at each pixel of each polygon, but the result is still clearly faceted:
- To get smoother-looking surfaces we use **vertex normals** at each vertex
 - Usually different from facet normal
 - Used **only** for shading
 - Think of as a better approximation of the **real** surface that the polygons approximate
- Vertex normals may be
 - Provided with the model
 - Approximated by averaging the normals of the facets that share the vertex



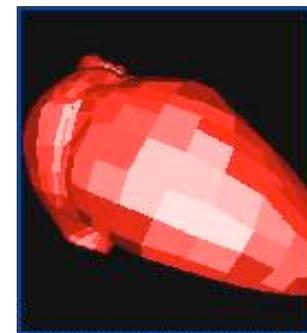
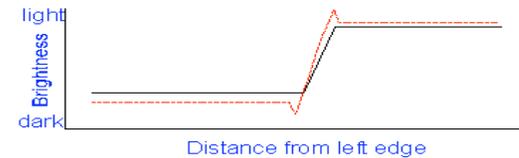
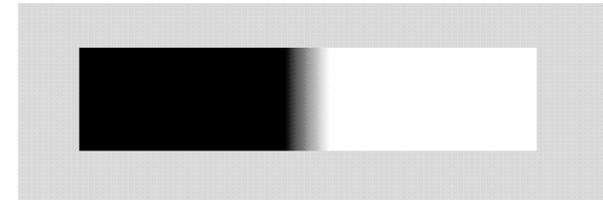
Gouraud Shading

- It directly illuminates or shades each vertex by using its location and normal.
- It linearly **interpolates** the resulting colors over faces: along bounding edges first, and then along scanlines in its interior.
- Advantages:
 - Fast - incremental calculations when rasterizing
 - Much smoother - use one normal per shared vertex to get continuity between faces
- Disadvantages:
 - Still inaccurate. Polygons appear dull and chalky.
 - It tends to eliminate the specular component. If included, it will be averaged over entire polygon.
 - Mach banding.

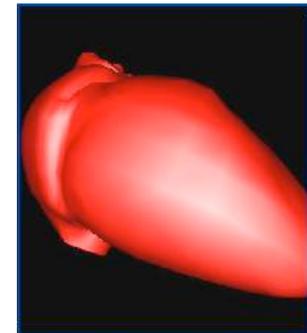


Gouraud Shading: Mach banding

- Artifact at discontinuities in intensity or intensity slope.
- The Mach banding describes an effect where the human mind subconsciously increase the contrast between two surfaces with different luminance.
- The difference between two colors is more pronounced when they are side by side and the boundary is smooth.
- This emphasizes boundaries between colors, even if the color difference is small.
- Rough boundaries are “averaged” by our vision system to give smooth variation



flat shading



Gouraud shading

*banded
along
edges*



floor appears banded



OpenGL shading

■ OpenGL defines two particular shading models:

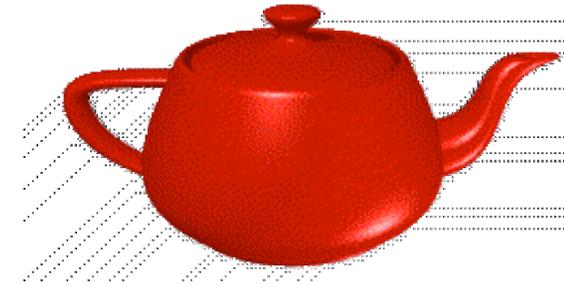
- Controls how colors are assigned to *pixels*
- **Gouraud shading**: *interpolates* between the colors at the *vertices* (the default)

```
glShadeModel(GL_SMOOTH)
```

- **Flat shading**: uses a *constant* color across the polygon

```
glShadeModel(GL_FLAT)
```

Phong Shading



- *Phong shading* is not the same as Phong lighting, though they are sometimes mixed up

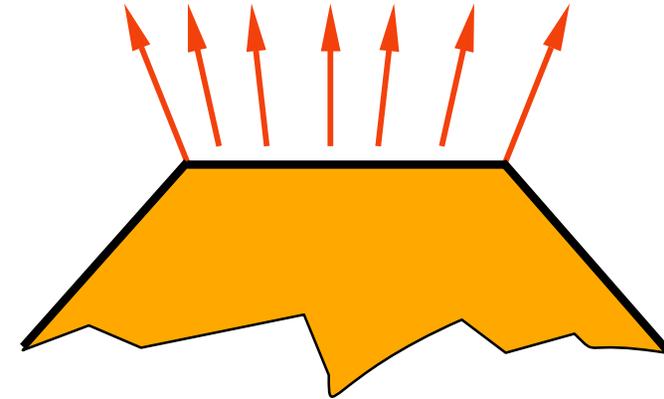
- **Phong lighting:** the empirical model we've been discussing to calculate illumination at a point on a surface
- **Phong shading:** linearly interpolates the surface normals across the facet, applying the Phong lighting model at every pixel

- **Advantages:**

- Usually very smooth-looking results
- High quality, narrow specularities

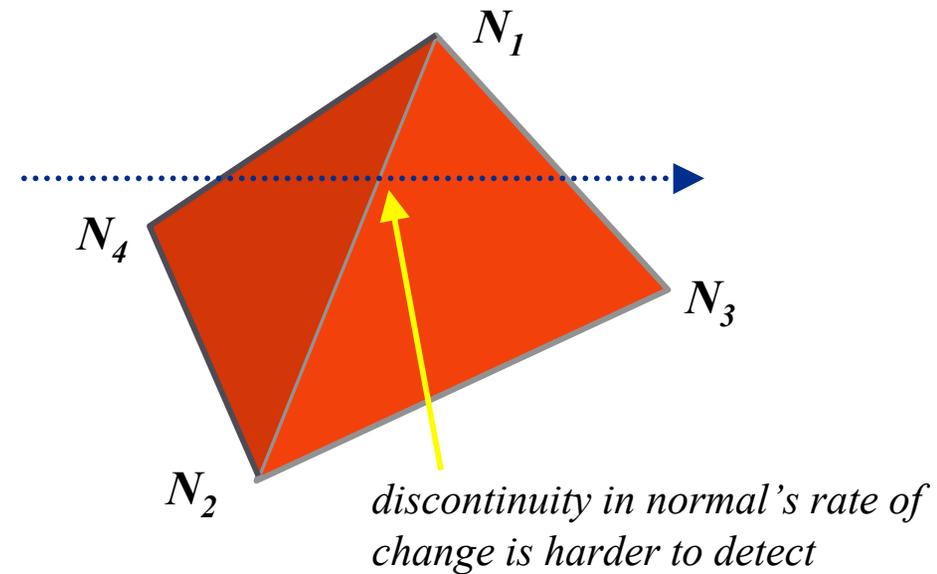
- **Disadvantages:**

- But, considerably more expensive
- Still an approximation for most surfaces



Phong Shading

- Linearly interpolate the vertex normals
 - Compute lighting equations at each pixel
 - Can use specular component
 - Note that normals are used to compute diffuse and specular terms



$$I_{total} = K_A I_A + \sum_{i=1}^{\# \text{ lights}} I_i (K_D (\vec{N} \cdot \vec{L}_i) + K_S (\vec{V} \cdot \vec{R}_i)^n)$$

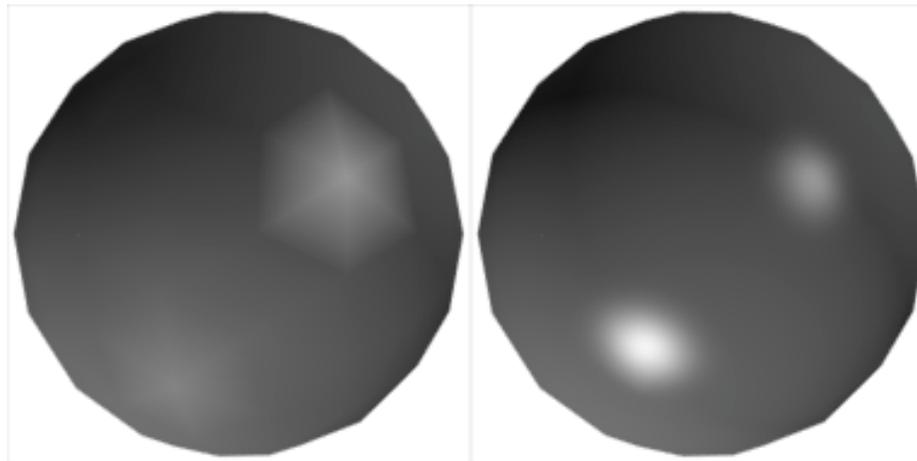


Shortcomings of Shading

- Polygonal silhouettes remain
- Perspective distortion
- Interpolation dependent on the polygon orientation
- Problems at shared vertices
- Bad vertex averaging

Shortcomings of Shading

- Polygonal silhouettes remain



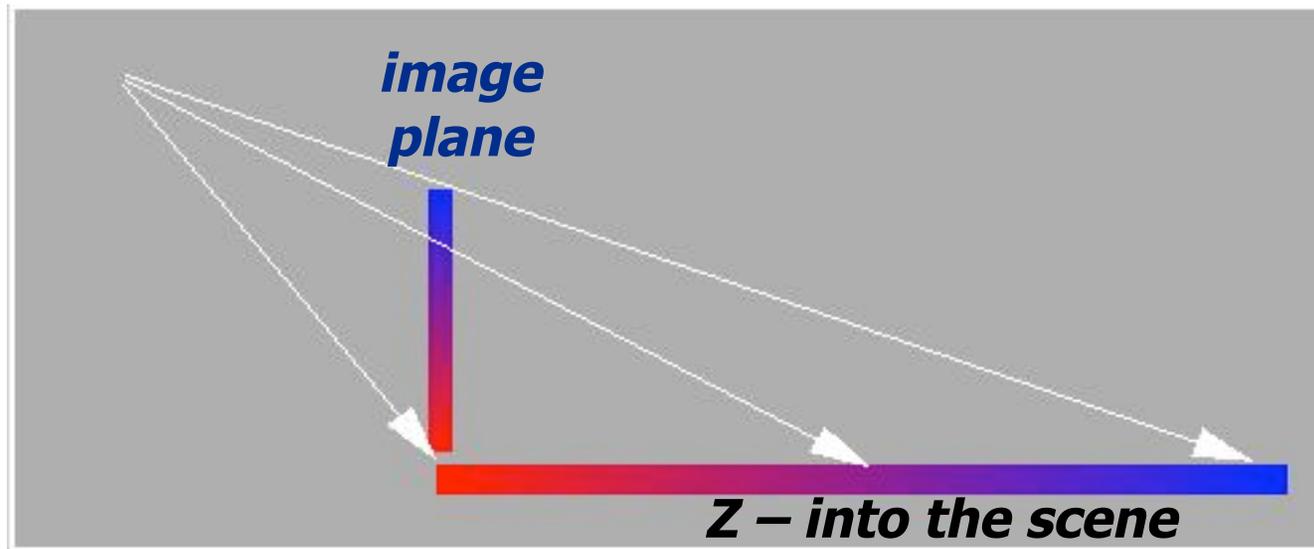
Gouraud

Phong

Shortcomings of Shading

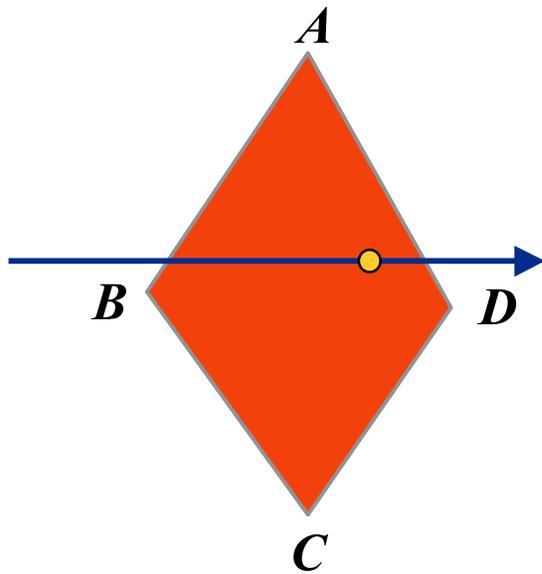
■ Perspective distortion

- Note that linear interpolation in screen space does not align with linear interpolation in world space.
- Break up large polygons with many smaller ones to reduce distortion.



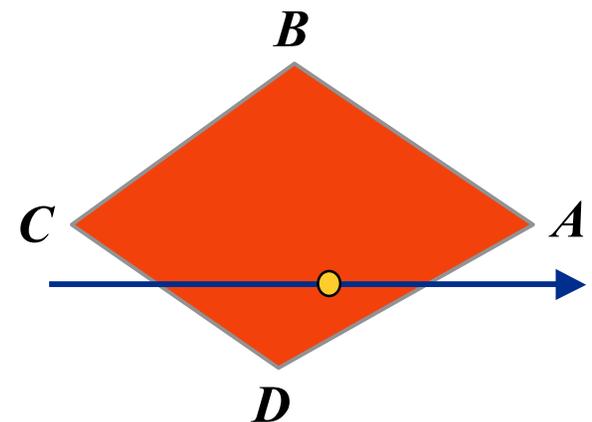
Shortcomings of Shading

- Interpolation dependent on the polygon orientation



***Interpolate between
AB and AD***

***Rotate -90°
and color
same point***



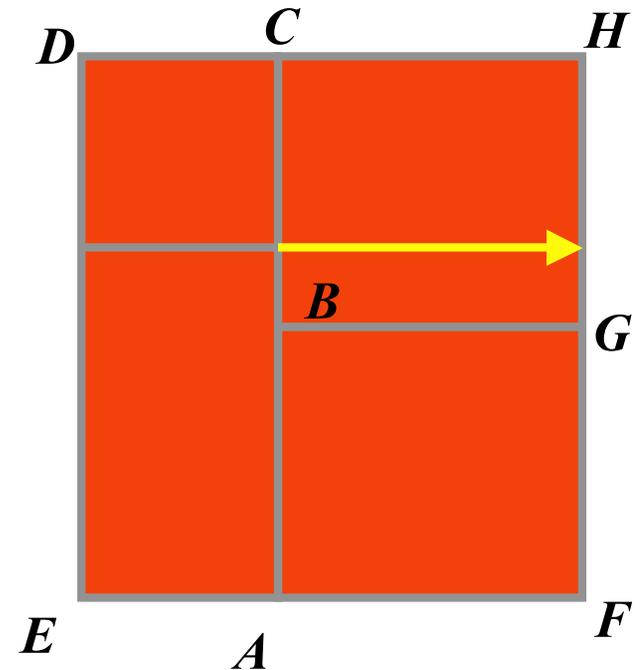
***Interpolate between
CD and AD***

Shortcomings of Shading

■ Problems at shared vertices

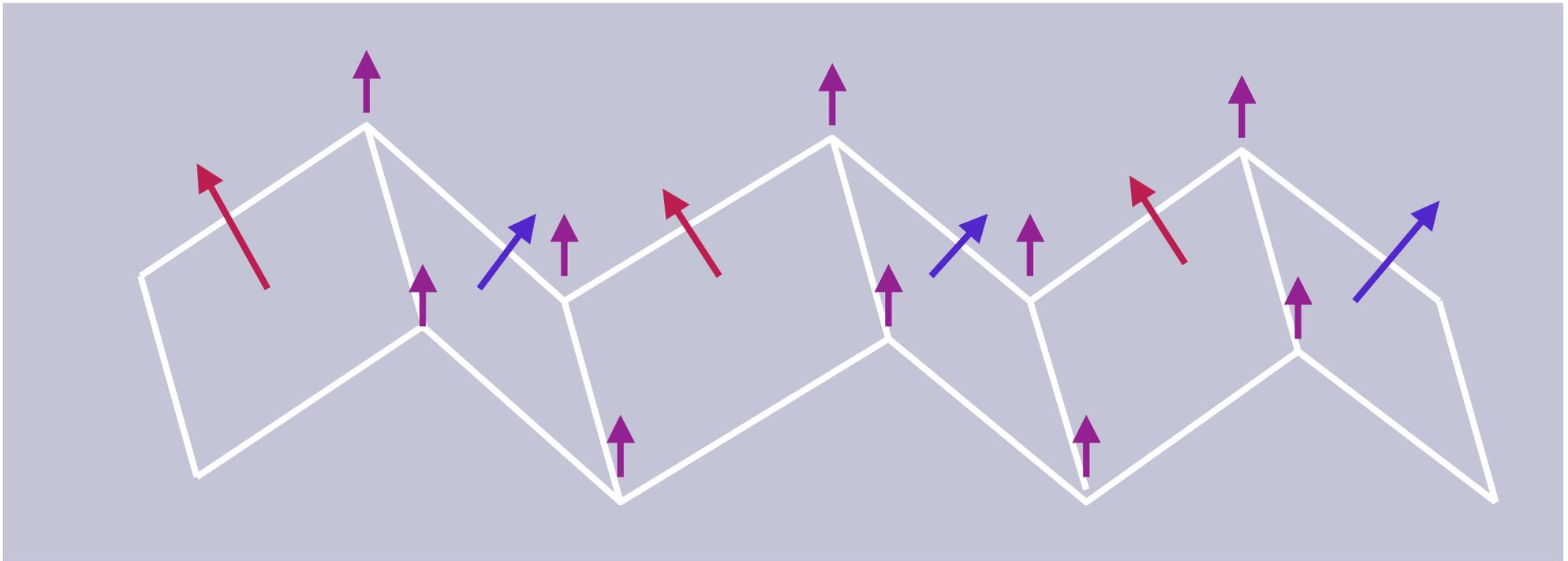
□ Example aside:

- The vertex B is shared by the two rectangles on the right, but not by the one on the left
- The first portion of the scanline is interpolated between DE and AC
- The second portion of the scanline is interpolated between BC and GH
- A large discontinuity could arise



Shortcomings of Shading

- Bad vertex averaging





Shading Models (Direct lighting)

summary

- Flat Shading
 - Compute Phong lighting once for entire polygon
- Gouraud Shading
 - Compute Phong lighting at the vertices and interpolate lighting values across polygon
- Phong Shading
 - Compute averaged vertex normals
 - Interpolate normals across polygon and perform Phong lighting across polygon



Current Generation of Shaders

- Current hardware allows you to break from the standard illumination model
- *Programmable Vertex Shaders* allow you to write a small program that determines how the color of a vertex is computed
 - Your program has access to the surface normal and position, plus anything else you care to give it (like the light)
 - You can add, subtract, take dot products, and so on



Current Generation of Shaders

- We have only touched on the complexities of illuminating surfaces
 - The common model is hopelessly inadequate for accurate lighting (but it's fast and simple)
- Consider two sub-problems of illumination
 - Where does the light go? *Light transport*
 - What happens at surfaces? *Reflectance models*
- Other algorithms address the transport or the reflectance problem, or both
 - Much later in class, or a separate course

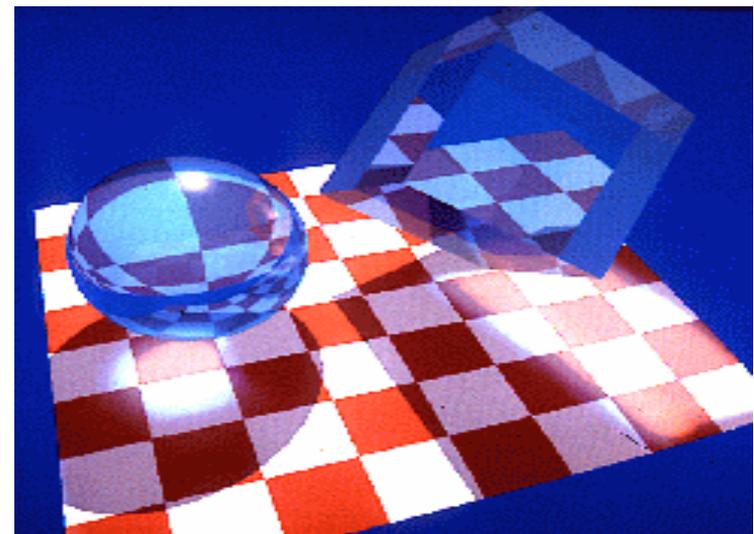
Overview: lighting-based models

■ Direct Illumination

- Emission at light sources
- Scattering at surfaces

■ Global Illumination

- Shadows
- Refractions
- Inter-object reflections





Global Illumination

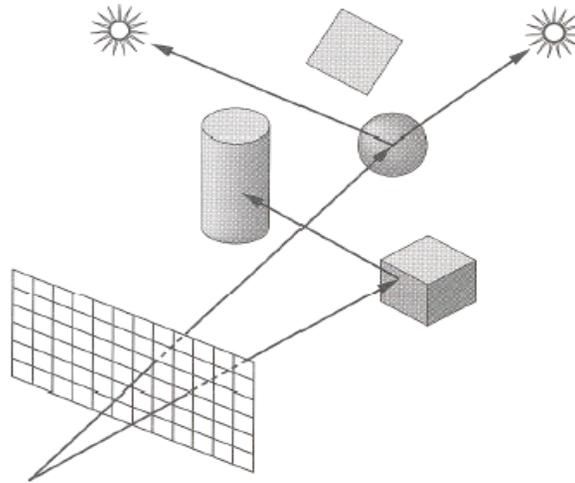
- We've glossed over how light really works
- And we will continue to do so...
- One step better

- Global Illumination
 - The notion that a point is illuminated by more than light from local lights; it is illuminated by all the emitters and reflectors in the global scene

Shadows

■ Shadow terms tell which light sources are blocked

- Cast ray towards each light source L_i
- $S_i = 0$ if ray is blocked, $S_i = 1$ otherwise



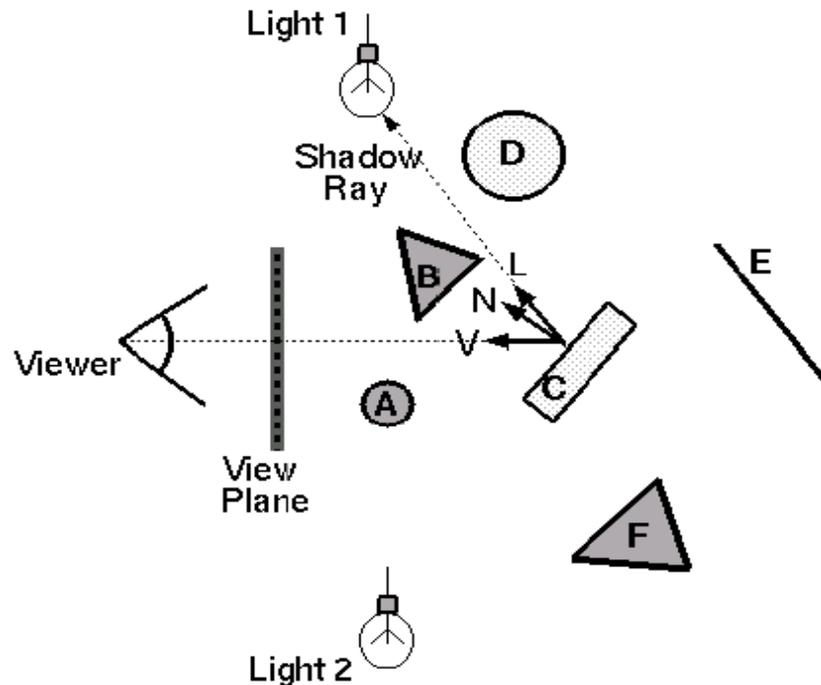
Shadow
Term

$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i$$

Ray Casting

- Trace **primary rays** from camera

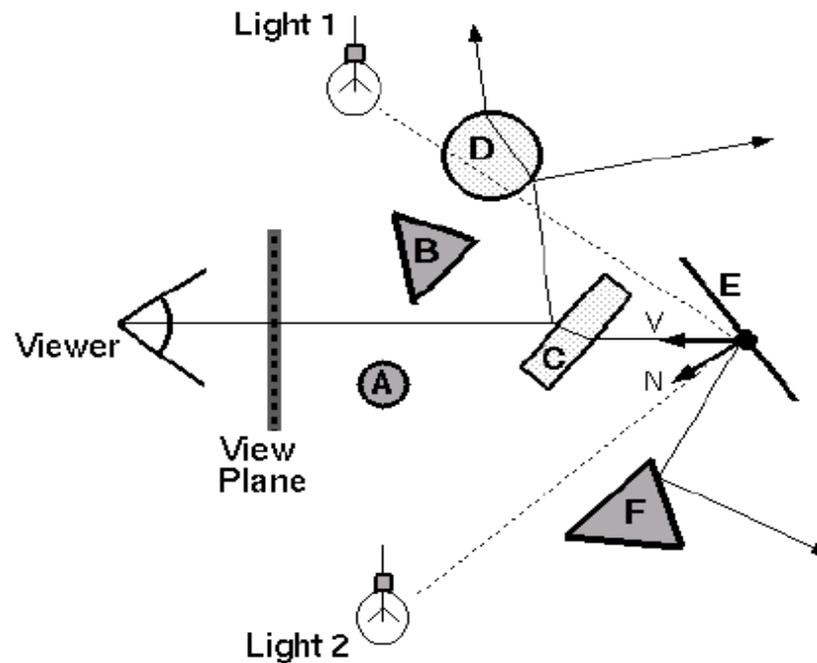
- Direct illumination from unblocked lights only



$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i$$

Recursive Ray Tracing

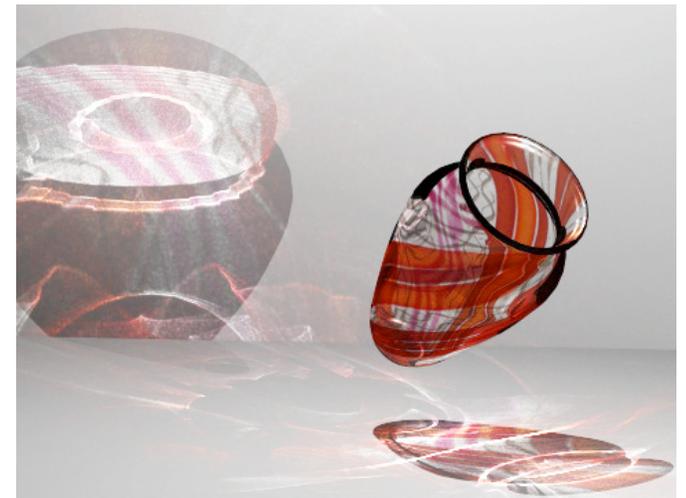
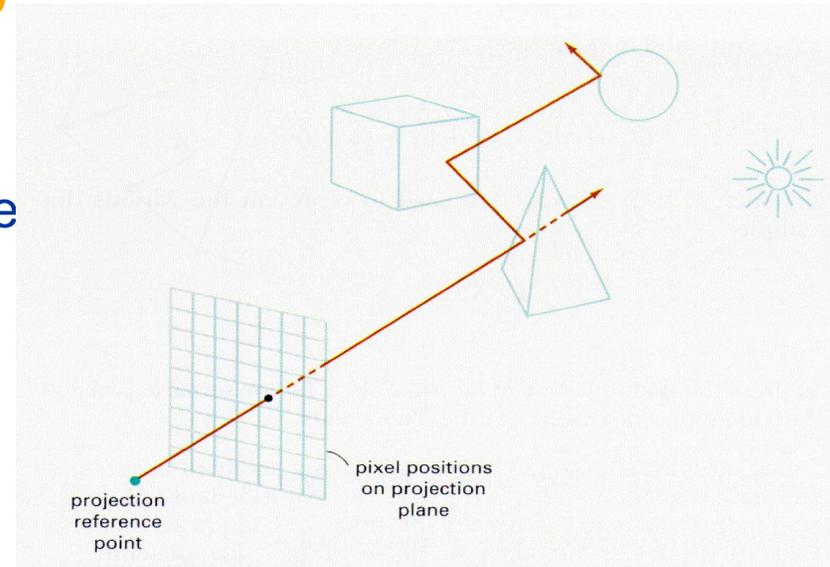
- Also trace **secondary rays** from hit surfaces
 - Global illumination from **mirror reflection** and **transparency**



$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i + K_S I_R + K_T I_T$$

Recursive Ray Tracing: overview

- **Primary rays.** Cast a ray from the viewer's eye through each pixel, and then from intersected object to light sources and determine shadow/lighting conditions
- **Secondary rays.** Also spawn secondary rays
 - Reflection rays and refraction rays
 - Use surface normal as guide (angle of incidence equals angle of reflection)
 - If another object is hit, determine the light it illuminates by recursing through ray tracing
- **Stop recursing when:**
 - ray fails to intersect an object
 - user-specified maximum depth is reached
 - system runs out of memory





Recursive Ray Tracing

■ Stop recursing when:

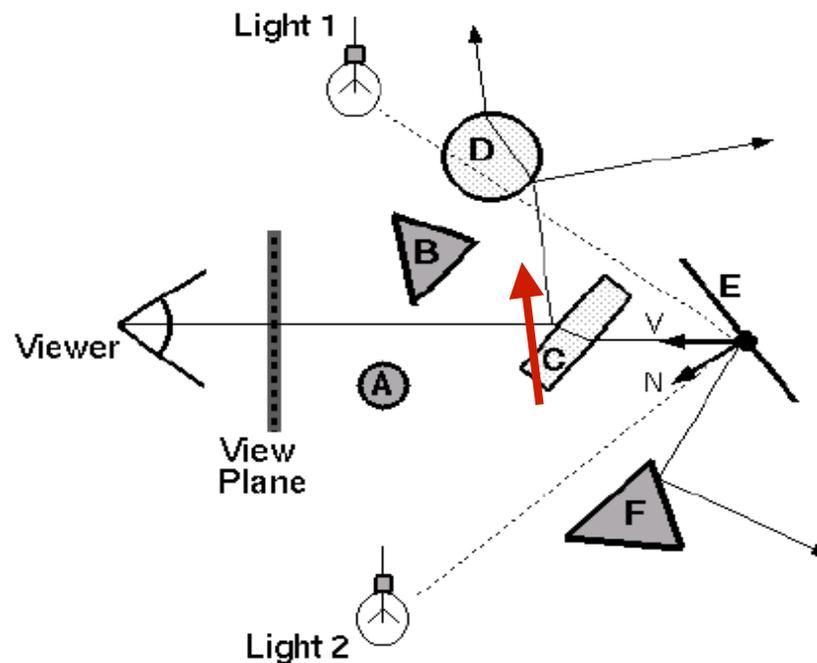
- ray fails to intersect an object
- user-specified maximum depth is reached
- system runs out of memory

■ Common numerical accuracy error

- Spawn secondary ray from intersection point
- Secondary ray intersects another polygon on same object

Mirror Reflection

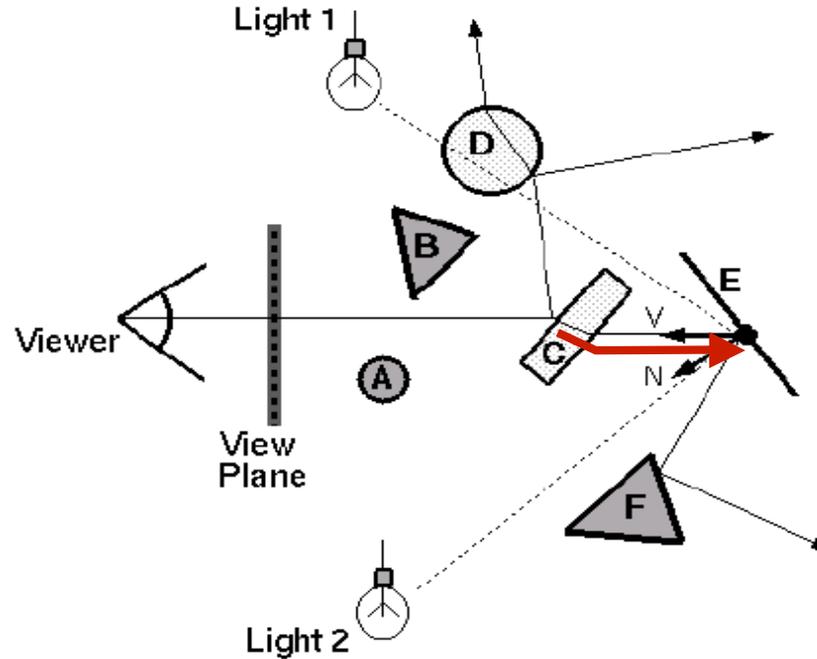
- Trace secondary ray in direction of mirror reflection
 - Evaluate radiance along secondary ray and include it into illumination model



$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i + K_S I_R + K_T I_T$$

Transparency

- Trace secondary ray in direction of refraction
 - Evaluate radiance along secondary ray and include it into illumination model

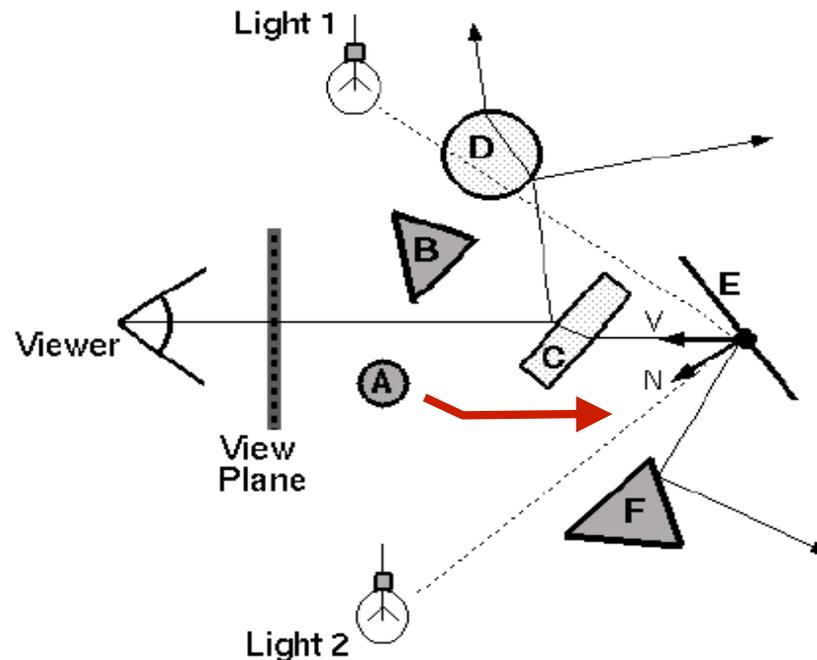


Radiance for refraction ray

$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i + K_S I_R + K_T I_T$$

Transparency

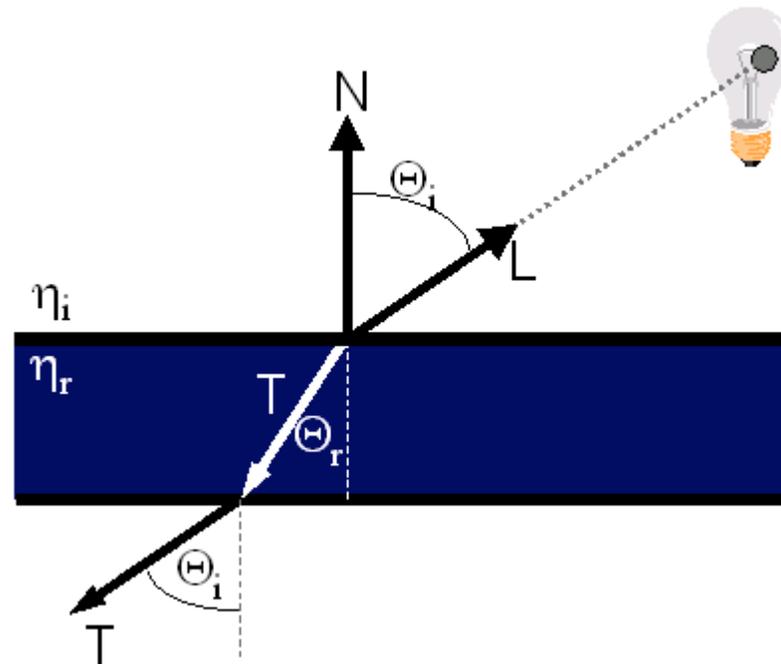
- Transparency coefficient is fraction transmitted
 - $K_T = 1$ if object is translucent, $K_T = 0$ if object is opaque
 - $0 < K_T < 1$ if object is semi-translucent



$$I = I_E + K_A I_A + \sum_{i=1}^{\# \text{ lights}} [K_D (\vec{N} \cdot \vec{L}) + K_S (\vec{V} \cdot \vec{R})^n] S_i I_i + K_S I_R + K_T I_T$$

Refractive Transparency

- For thin surfaces, can ignore change in direction
 - Assume light travels straight through surface

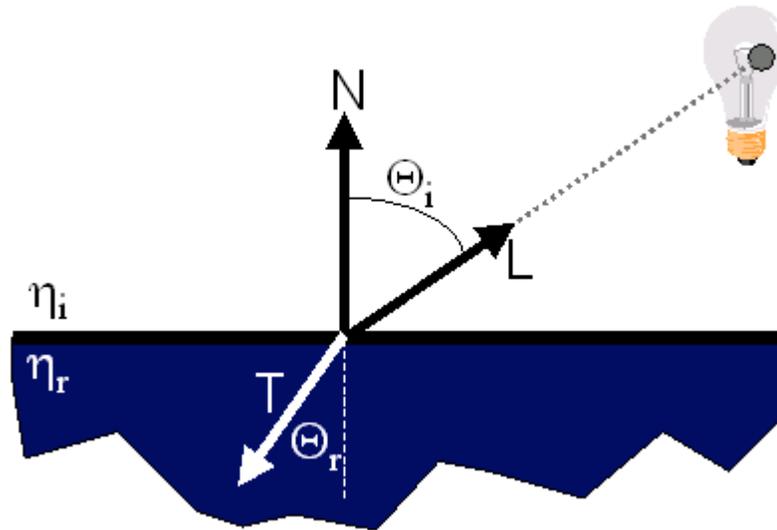


$$T \cong -L$$

Refractive Transparency

■ For solid objects, apply Snell's Law:

□ $\eta_r \sin \Theta_r = \eta_i \sin \Theta_i$

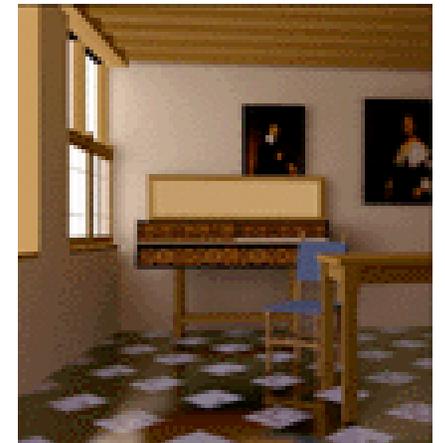


$$T = \left(\frac{\eta_i}{\eta_r} \cos \Theta_i - \cos \Theta_r \right) N - \frac{\eta_i}{\eta_r} L$$

Radiosity



- Ray tracing models specular reflection and refractive transparency, but still uses an ambient term to account for other lighting effects
- Radiosity is the rate at which energy is emitted or reflected by a surface
- By conserving light energy in a volume, these radiosity effects can be traced





Summary

- Direct Illumination-based Shading

- Ray casting

- Usually use simple analytic approximations for light source emission and surface reflectance

- Indirect illumination-based Shading

- Recursive ray tracing

- Incorporate shadows, mirror reflections, and pure refractions

- Radiosity

- Use energy conservative law.