

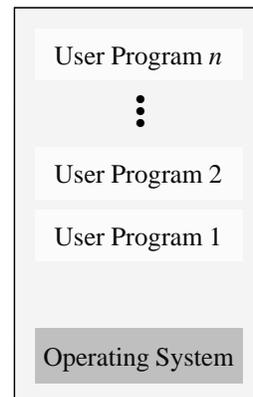
# *Page Replacement Algorithms*

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## **Virtual Memory Management**

### **Fundamental issues : A Recap**

- ◆ Key concept: Demand paging
  - Load pages into memory only when a page fault occurs
- ◆ Issues:
  - Placement strategies
    - ❖ Place pages anywhere – no placement policy required
  - Replacement strategies
    - ❖ What to do when there exist more jobs than can fit in memory
  - Load control strategies
    - ❖ Determining how many jobs can be in memory at one time



Memory

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## Page Replacement Algorithms

### Concept

- ◆ Typically  $\sum_i VAS_i \gg \text{Physical Memory}$
- ◆ With demand paging, physical memory fills quickly
- ◆ When a process faults & memory is full, some page must be swapped out
  - Handling a page fault now requires **2** disk accesses not 1!
  - Though writes are more efficient than reads (why?)

Which page should be replaced?

*Local replacement* — Replace a page of the faulting process

*Global replacement* — Possibly replace the page of another process

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## Page Replacement Algorithms

### Evaluation methodology

- ◆ Record a *trace* of the pages accessed by a process
  - Example: (Virtual) address trace...  
(3,0), (1,9), (4,1), (2,1), (5,3), (2,0), (1,9), (2,4), (3,1), (4,8)
  - generates page trace  
3, 1, 4, 2, 5, 2, 1, 2, 3, 4 (represented as c, a, d, b, e, b, a, b, c, d)
- ◆ Hardware can tell OS when a new page is loaded into the TLB
  - Set a used bit in the page table entry
  - Increment or shift a register

Simulate the behavior of a page replacement algorithm on the trace and record the number of page faults generated

*fewer faults*  $\Rightarrow$  *better performance*

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### Optimal Page Replacement Clairvoyant replacement

- ◆ Replace the page that won't be needed for the longest time in the future

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>									
	1	<i>b</i>									
	2	<i>c</i>									
	3	<i>d</i>									
Faults											
Time page needed next											

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### Optimal Page Replacement Clairvoyant replacement

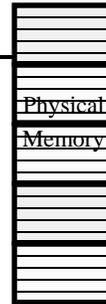
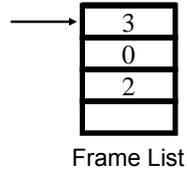
- ◆ Replace the page that won't be needed for the longest time in the future

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>d</i>
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>
	3	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>
Faults						•					•
Time page needed next					<i>a</i> = 7 <i>b</i> = 6 <i>c</i> = 9 <i>d</i> = 10				<i>a</i> = 15 <i>b</i> = 11 <i>c</i> = 13 <i>d</i> = 14		

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## Local Page Replacement FIFO replacement

- ◆ Simple to implement
  - A single pointer suffices



- ◆ Performance with 4 page frames:

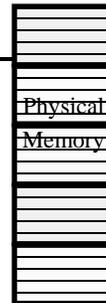
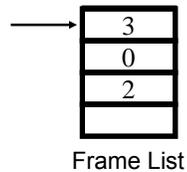
Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>									
	1	<i>b</i>									
	2	<i>c</i>									
	3	<i>d</i>									
Faults											



7

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Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>d</i>
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>
	2	<i>c</i>	<i>b</i>	<i>b</i>	<i>b</i>						
	3	<i>d</i>	<i>c</i>	<i>c</i>							
Faults						•		•	•	•	•

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## Least Recently Used Page Replacement

Use the recent past as a predictor of the near future

- ◆ Replace the page that hasn't been referenced for the longest time

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>									
	1	<i>b</i>									
	2	<i>c</i>									
	3	<i>d</i>									
Faults											
Time page last used											



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## Least Recently Used Page Replacement

Use the recent past as a predictor of the near future

- ◆ Replace the page that hasn't been referenced for the longest time

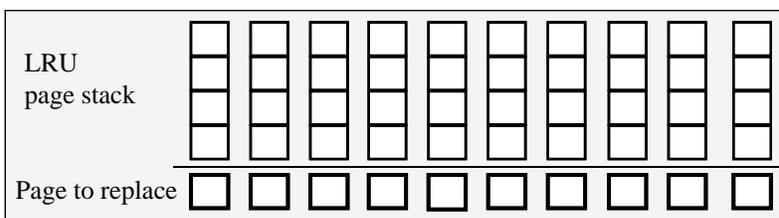
Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>d</i>
	3	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>c</i>	<i>c</i>
Faults						•				•	•
Time page last used					<i>a</i> = 2 <i>b</i> = 4 <i>c</i> = 1 <i>d</i> = 3			<i>a</i> = 7 <i>b</i> = 8 <i>e</i> = 5 <i>d</i> = 3	<i>a</i> = 7 <i>b</i> = 8 <i>e</i> = 5 <i>c</i> = 9		

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## Least Recently Used Page Replacement Implementation

- Maintain a "stack" of recently used pages

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>									
1	<i>b</i>										
2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>d</i>
3	<i>d</i>	<i>c</i>	<i>c</i>								
Faults						•				•	•

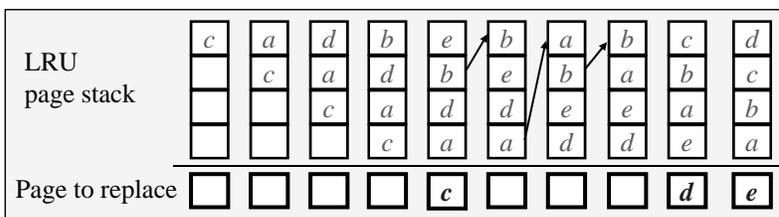


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## Least Recently Used Page Replacement Implementation

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Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>									
1	<i>b</i>										
2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>d</i>
3	<i>d</i>	<i>c</i>	<i>c</i>								
Faults						•				•	•

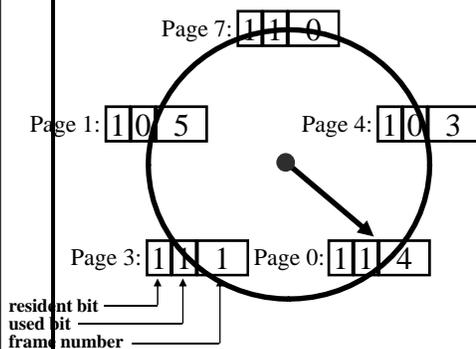


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- ◆ What is the goal of a page replacement algorithm?
  - A. Make life easier for OS implementer
  - B. Reduce the number of page faults
  - C. Reduce the penalty for page faults when they occur
  - D. Minimize CPU time of algorithm

## Approximate LRU Page Replacement The *Clock* algorithm

- ◆ Maintain a circular list of pages resident in memory
  - Use a *clock* (or *used/referenced*) bit to track how often a page is accessed
  - The bit is set whenever a page is referenced
- ◆ Clock hand sweeps over pages looking for one with *used* bit = 0
  - Replace pages that haven't been referenced for one complete revolution of the clock



```

func Clock_Replacement
begin
  while (victim page not found) do
    if (used bit for current page = 0) then
      replace current page
    else
      reset used bit
    end if
    advance clock pointer
  end while
end Clock_Replacement

```

### Clock Page Replacement Example

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>						
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>						
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>						
	3	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>						
Faults											

Page table entries for resident pages:

1	<i>a</i>
1	<i>b</i>
1	<i>c</i>
1	<i>d</i>

### Clock Page Replacement Example

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>e</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>d</i>
	1	<i>b</i>									
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>
	3	<i>d</i>	<i>c</i>	<i>c</i>							
Faults						•		•		•	•

Page table entries for resident pages:

1	<i>a</i>
1	<i>b</i>
1	<i>c</i>
1	<i>d</i>

1	<i>e</i>
0	<i>b</i>
0	<i>c</i>
0	<i>d</i>

1	<i>e</i>
1	<i>b</i>
0	<i>c</i>
0	<i>d</i>

1	<i>e</i>
0	<i>b</i>
1	<i>a</i>
0	<i>d</i>

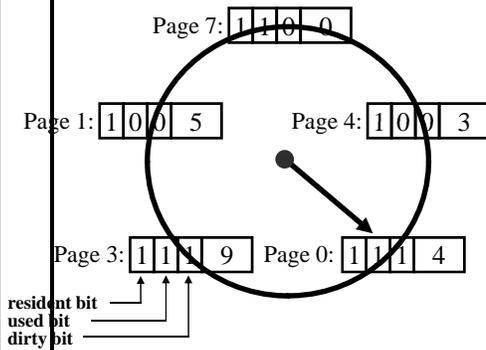
1	<i>e</i>
1	<i>b</i>
1	<i>a</i>
0	<i>d</i>

1	<i>e</i>
1	<i>b</i>
1	<i>a</i>
1	<i>c</i>

1	<i>d</i>
0	<i>b</i>
0	<i>a</i>
0	<i>c</i>

## Optimizing Approximate LRU Replacement The Second Chance algorithm

- There is a significant cost to replacing “dirty” pages
- Modify the Clock algorithm to allow dirty pages to always survive one sweep of the clock hand
  - Use both the *dirty bit* and the *used bit* to drive replacement



### Second Chance Algorithm

Before clock sweep		After clock sweep	
<i>used</i>	<i>dirty</i>	<i>used</i>	<i>dirty</i>
0	0		
0	1	0	0
1	0	0	0
1	1	0	1

*replace page*

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## The Second Chance Algorithm Example

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>a<sup>w</sup></i>	<i>d</i>	<i>b<sup>w</sup></i>	<i>e</i>	<i>b</i>	<i>a<sup>w</sup></i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>						
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>						
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>						
	3	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>						
Faults											

Page table entries for resident pages:

10	<i>a</i>						
10	<i>b</i>						
10	<i>c</i>						
10	<i>d</i>						

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The Second Chance Algorithm Example																																																															
Time	0	1	2	3	4	5	6	7	8	9	10																																																				
Requests		<i>c</i>	<i>a<sup>w</sup></i>	<i>d</i>	<i>b<sup>w</sup></i>	<i>e</i>	<i>b</i>	<i>a<sup>w</sup></i>	<i>b</i>	<i>c</i>	<i>d</i>																																																				
Page Frames	0	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>																																																				
	1	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>b</i>	<i>d</i>																																																				
	2	<i>c</i>	<i>c</i>	<i>c</i>	<i>c</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>	<i>e</i>																																																				
	3	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>d</i>	<i>c</i>	<i>c</i>																																																				
Faults						•				•	•																																																				
Page table entries for resident pages:	<table border="1"> <tr><td>10</td><td><i>a</i></td></tr> <tr><td>10</td><td><i>b</i></td></tr> <tr><td>10</td><td><i>c</i></td></tr> <tr><td>10</td><td><i>d</i></td></tr> </table>	10	<i>a</i>	10	<i>b</i>	10	<i>c</i>	10	<i>d</i>	<table border="1"> <tr><td>11</td><td><i>a</i></td></tr> <tr><td>11</td><td><i>b</i></td></tr> <tr><td>10</td><td><i>c</i></td></tr> <tr><td>10</td><td><i>d</i></td></tr> </table>	11	<i>a</i>	11	<i>b</i>	10	<i>c</i>	10	<i>d</i>	<table border="1"> <tr><td>00</td><td><i>a</i>*</td></tr> <tr><td>00</td><td><i>b</i>*</td></tr> <tr><td>10</td><td><i>e</i></td></tr> <tr><td>00</td><td><i>d</i></td></tr> </table>	00	<i>a</i> *	00	<i>b</i> *	10	<i>e</i>	00	<i>d</i>	<table border="1"> <tr><td>00</td><td><i>a</i></td></tr> <tr><td>10</td><td><i>b</i></td></tr> <tr><td>10</td><td><i>e</i></td></tr> <tr><td>00</td><td><i>d</i></td></tr> </table>	00	<i>a</i>	10	<i>b</i>	10	<i>e</i>	00	<i>d</i>	<table border="1"> <tr><td>11</td><td><i>a</i></td></tr> <tr><td>10</td><td><i>b</i></td></tr> <tr><td>10</td><td><i>e</i></td></tr> <tr><td>00</td><td><i>d</i></td></tr> </table>	11	<i>a</i>	10	<i>b</i>	10	<i>e</i>	00	<i>d</i>	<table border="1"> <tr><td>11</td><td><i>a</i></td></tr> <tr><td>10</td><td><i>b</i></td></tr> <tr><td>10</td><td><i>e</i></td></tr> <tr><td>10</td><td><i>c</i></td></tr> </table>	11	<i>a</i>	10	<i>b</i>	10	<i>e</i>	10	<i>c</i>	<table border="1"> <tr><td>00</td><td><i>a</i>*</td></tr> <tr><td>10</td><td><i>d</i></td></tr> <tr><td>00</td><td><i>e</i></td></tr> <tr><td>00</td><td><i>c</i></td></tr> </table>	00	<i>a</i> *	10	<i>d</i>	00	<i>e</i>	00	<i>c</i>
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The Problem With Local Page Replacement How much memory do we allocate to a process?													
Time	0	1	2	3	4	5	6	7	8	9	10	11	12
Requests		<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>
Page Frames	0	<i>a</i>											
	1	<i>b</i>											
	2	<i>c</i>											
Faults													
Page Frames	0	<i>a</i>											
	1	<i>b</i>											
	2	<i>c</i>											
	3	-											
Faults													

## The Problem With Local Page Replacement

How much memory do we allocate to a process?

Time	0	1	2	3	4	5	6	7	8	9	10	11	12
Requests		a	b	c	d	a	b	c	d	a	b	c	d

Page Frames	0	a	a	a	a	(d)	d	d	(c)	c	c	(b)	b	b
	1	b	b	b	b	b	(a)	a	a	(d)	d	d	(c)	c
	2	c	c	c	c	c	c	(b)	b	b	(a)	a	a	(d)
Faults						•	•	•	•	•	•	•	•	•

Page Frames	0	a	a	a	a	a	a	a	a	a	a	a	a	a
	1	b	b	b	b	b	b	b	b	b	b	b	b	b
	2	c	c	c	c	c	c	c	c	c	c	c	c	c
	3	-				(d)	d	d	d	d	d	d	d	d
Faults						•								

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## Page Replacement Algorithms

### Performance

- ◆ Local page replacement
  - LRU — Ages pages based on when they were last used
  - FIFO — Ages pages based on when they're brought into memory
- ◆ Towards global page replacement ... with variable number of page frames allocated to processes

### The principle of locality

- 90% of the execution of a program is sequential
- Most iterative constructs consist of a relatively small number of instructions
- When processing large data structures, the dominant cost is sequential processing on individual structure elements
- Temporal vs. physical locality

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## Optimal Page Replacement

For processes with a variable number of frames

- ◆ *VMIN* — Replace a page that is not referenced in the *next*  $\tau$  accesses
- ◆ Example:  $\tau = 4$

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	• $t=0$									
	Page <i>b</i>	-									
	Page <i>c</i>	-									
	Page <i>d</i>	• $t=-1$									
	Page <i>e</i>	-									
Faults											



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## Optimal Page Replacement

For processes with a variable number of frames

- ◆ *VMIN* — Replace a page that is not referenced in the *next*  $\tau$  accesses
- ◆ Example:  $\tau = 4$

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	• $t=0$	-	-	-	-	-	-	-	( <i>F</i> )	-
	Page <i>b</i>	-	-	-	( <i>F</i> )	-	-	-	-	-	-
	Page <i>c</i>	-	( <i>F</i> )	•	•	•	•	•	•	-	-
	Page <i>d</i>	• $t=-1$	•	•	•	-	-	-	-	-	( <i>F</i> )
	Page <i>e</i>	-	-	-	-	-	-	( <i>F</i> )	•	•	-
Faults		•			•		•			•	•

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## Explicitly Using Locality

### The working set model of page replacement

- ◆ Assume recently referenced pages are likely to be referenced again soon...
- ◆ ... and *only* keep those pages recently referenced in memory (called *the working set*)
  - Thus pages may be removed even when no page fault occurs
  - The number of frames allocated to a process will vary over time
- ◆ A process is allowed to execute only if its working set fits into memory
  - The working set model performs implicit load control

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## Working Set Page Replacement Implementation

- ◆ Keep track of the last  $\tau$  references
  - The pages referenced during the last  $\tau$  memory accesses are the working set
  - $\tau$  is called the *window size*
- ◆ Example: Working set computation,  $\tau = 4$  references:

Time		0	1	2	3	4	5	6	7	8	9	10
Requests			<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	$\bullet$ $t=0$										
	Page <i>b</i>	-										
	Page <i>c</i>	-										
	Page <i>d</i>	$\bullet$ $t=-1$										
	Page <i>e</i>	$\bullet$ $t=-2$										
Faults												

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## Working Set Page Replacement Implementation

- ◆ Keep track of the last  $\tau$  references
  - The pages referenced during the last  $\tau$  memory accesses are the working set
  - $\tau$  is called the *window size*
- ◆ Example: Working set computation,  $\tau = 4$  references:
  - What if  $\tau$  is too small? too large?

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	$t=0$	•	•	•	-	-	-	-	(F)	•
	Page <i>b</i>	-	-	-	(F)	•	•	•	•	-	-
	Page <i>c</i>	-	(F)	•	•	•	•	•	•	•	•
	Page <i>d</i>	$t=-1$	•	•	•	•	•	-	-	-	(F)
	Page <i>e</i>	$t=-2$	•	-	-	-	-	(F)	•	•	•
Faults		•			•		•			•	•

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## Page-Fault-Frequency Page Replacement An alternate working set computation

- ◆ Explicitly attempt to minimize page faults
  - When page fault frequency is high — *increase working set*
  - When page fault frequency is low — *decrease working set*

### Algorithm:

Keep track of the rate at which faults occur  
 When a fault occurs, compute the time since the last page fault  
 Record the time,  $t_{last}$ , of the last page fault  
 If the time between page faults is "large" then reduce the working set  
 If  $t_{current} - t_{last} > \tau$ , then remove from memory all pages not referenced in  $[t_{last}, t_{current}]$   
 If the time between page faults is "small" then increase working set  
 If  $t_{current} - t_{last} \leq \tau$ , then add faulting page to the working set

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### Page-Fault-Frequency Page Replacement

Example, window size = 2

- If  $t_{current} - t_{last} > 2$ , remove pages not referenced in  $[t_{last}, t_{current}]$  from the working set
- If  $t_{current} - t_{last} \leq 2$ , just add faulting page to the working set

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	•									
	Page <i>b</i>	-									
	Page <i>c</i>	-									
	Page <i>d</i>	•									
	Page <i>e</i>	•									
Faults											
$t_{cur} - t_{last}$											



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### Page-Fault-Frequency Page Replacement

Example, window size = 2

- If  $t_{current} - t_{last} > 2$ , remove pages not referenced in  $[t_{last}, t_{current}]$  from the working set
- If  $t_{current} - t_{last} \leq 2$ , just add faulting page to the working set

Time	0	1	2	3	4	5	6	7	8	9	10
Requests		<i>c</i>	<i>c</i>	<i>d</i>	<i>b</i>	<i>c</i>	<i>e</i>	<i>c</i>	<i>e</i>	<i>a</i>	<i>d</i>
Pages in Memory	Page <i>a</i>	•	•	•	-	-	-	-	-	(F)	•
	Page <i>b</i>	-	-	-	(F)	•	•	•	•	-	-
	Page <i>c</i>	-	(F)	•	•	•	•	•	•	•	•
	Page <i>d</i>	•	•	•	•	•	•	•	•	-	(F)
	Page <i>e</i>	•	•	•	-	-	(F)	•	•	•	•
Faults		•			•		•			•	•
$t_{cur} - t_{last}$		1			3		2			3	1

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## Load Control

### Fundamental tradeoff

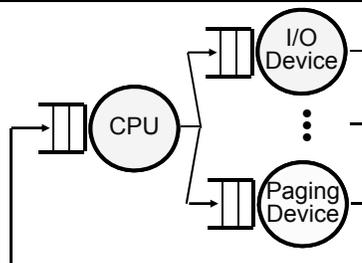
- ◆ High multiprogramming level
  - $MPL_{max} = \frac{\text{number of page frames}}{\text{minimum number of frames required for a process to execute}}$
- ◆ Low paging overhead
  - $MPL_{min} = 1$  process
- ◆ Issues
  - What criterion should be used to determine when to increase or decrease the  $MPL$ ?
  - Which task should be swapped out if the  $MPL$  must be reduced?

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## Load Control

### How *not* to do it: Base load control on CPU utilization

- ◆ Assume memory is nearly full
- ◆ A chain of page faults occur
  - A queue of processes forms at the paging device
- ◆ CPU utilization falls
- ◆ Operating system increases  $MPL$ 
  - New processes fault, taking memory away from existing processes
- ◆ CPU utilization goes to 0, the OS increases the  $MPL$  further...



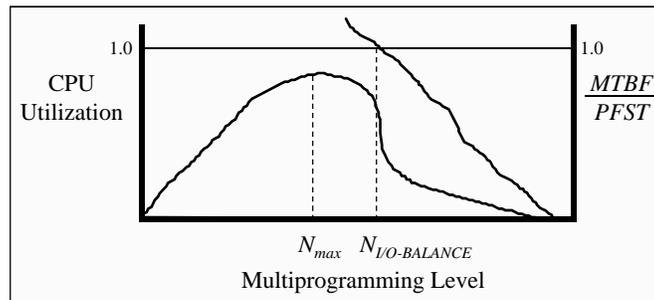
System is *thrashing* — spending all of its time paging

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## Load Control

### Thrashing

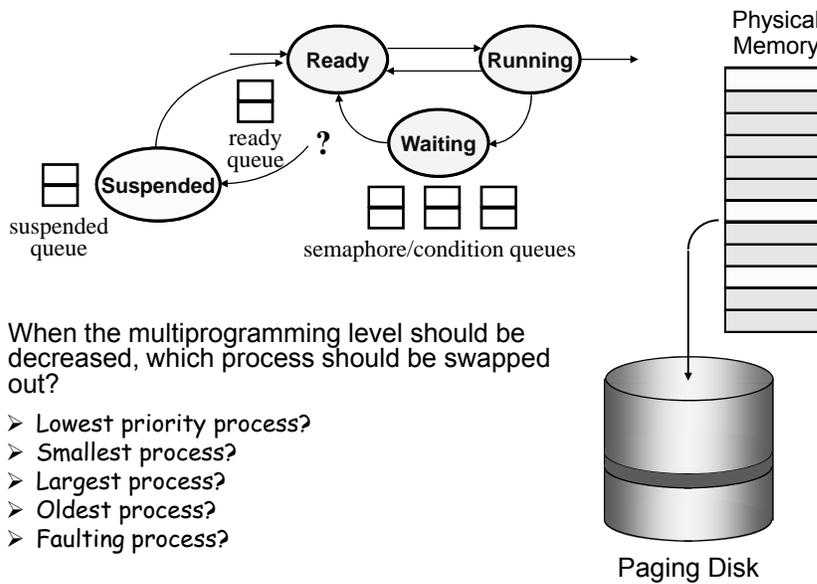
- ◆ Thrashing can be ameliorated by *local* page replacement
- ◆ Better criteria for load control: Adjust MPL so that:
  - mean time between page faults ( $MTBF$ ) = page fault service time ( $PFST$ )
  - $\sum WS_i = \text{size of memory}$



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## Load Control

### Thrashing



- ◆ When the multiprogramming level should be decreased, which process should be swapped out?
  - Lowest priority process?
  - Smallest process?
  - Largest process?
  - Oldest process?
  - Faulting process?

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